

4.50  $P = 900 \text{ N}$ ,  $Q = 4000 \text{ N}$ ,  $T = 1950 \text{ N}$ ,  $a = 2.1 \text{ m}$ ,  $b = 3 \text{ m}$ ,  $c = 7.2 \text{ m}$

$$\alpha = \tan^{-1} \frac{7.2}{3} = \tan^{-1}(2.4) = 67.38^\circ$$

$$\overline{BC} = \sqrt{3^2 + 7.2^2} = 7.8 \text{ (m)}$$

(a) S; known  $P, Q, a, b, c$   
 unknown reaction **C, A**  
 유형 1&2 (줄, 힌지)  
 method 힘의 평형, 모멘트 평형

$$\begin{aligned} \text{A; } +\curvearrowright \Sigma M_B = 0; \quad c A_x - a P = 0 \\ \Rightarrow A_x = \frac{a}{c} P = \frac{2.1}{7.2} (900 \text{ N}) = 262.5 \text{ N} \end{aligned}$$

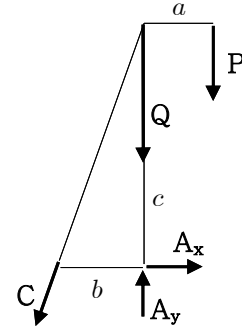
$$\begin{aligned} \Sigma F_x = 0; \quad -T \cos \alpha + A_x = 0 \\ \Rightarrow T = \frac{7.8}{3} A_x = 2.6 (262.5 \text{ N}) = 682.5 \text{ N} \end{aligned}$$

$$\begin{aligned} \Sigma F_y = 0; \quad A_y - T \sin \alpha - (P + Q) = 0 \\ \Rightarrow A_y = \frac{7.2}{7.8} T + P + Q = \frac{12}{13} (682.5 \text{ N}) + (4900 \text{ N}) = 5530 \text{ N} \end{aligned}$$

$$A = \sqrt{A_x^2 + A_y^2} = \sqrt{(262.5)^2 + (5530)^2} = 5536 \text{ N}$$

$$\theta = \tan^{-1} \frac{A_y}{A_x} = \tan^{-1} \frac{5530}{262.5} = \tan^{-1}(21.07) = 87.28^\circ$$

M; 자유물체도(F.B.D.)



$$\Rightarrow C = 683 \text{ N } \nearrow 67.4^\circ$$

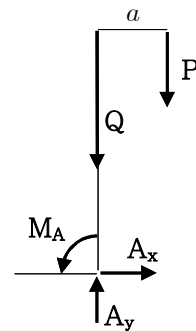
(b) S; known  $P, Q, a$   
 unknown reaction **A, M<sub>A</sub>**  
 유형 3 (고정)  
 method 힘의 평형, 모멘트 평형

$$\begin{aligned} \text{A; } +\curvearrowright \Sigma M_A = 0; \quad M_A - a P = 0 \\ \Rightarrow M_A = a P = (2.1 \text{ m}) (900 \text{ N}) = 1890.0 \text{ N} \cdot \text{m} \\ \Rightarrow M_A = 1890 \text{ N} \cdot \text{m } \curvearrowright \end{aligned}$$

$$\Sigma F_x = 0; \quad A_x = 0$$

$$\begin{aligned} \Sigma F_y = 0; \quad A_y - (P + Q) = 0 \\ \Rightarrow A_y = P + Q = 4900 \text{ N} \end{aligned}$$

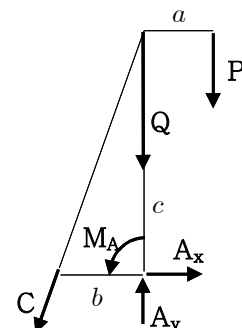
M; 자유물체도(F.B.D.)



$$\Rightarrow A = 4900 \text{ N } \uparrow$$

(c) S; known  $P, Q, T, a, b, c$   
 unknown reaction **C, A, M<sub>A</sub>**  
 유형 1&3 (줄, 고정)  
 method 힘의 평형, 모멘트 평형

M; 자유물체도(F.B.D.)



$$A; \mathbf{C} = \mathbf{T} = 1950 \text{ N } \nearrow 67.4^\circ \quad \Rightarrow \quad \mathbf{C} = 1950 \text{ N } \nearrow 67.4^\circ$$

$$\Sigma F_x = 0; \quad -T \cos \alpha + A_x = 0$$

$$\Rightarrow A_x = T \cos \alpha = (1950 \text{ N}) \frac{3}{7.8} = 750 \text{ N}$$

$$\Sigma F_y = 0; \quad A_y - T \sin \alpha - (P+Q) = 0$$

$$\Rightarrow A_y = \frac{7.2}{7.8} T + P + Q = \frac{12}{13} (1950 \text{ N}) + (4900 \text{ N}) = 6700 \text{ N}$$

$$A = \sqrt{A_x^2 + A_y^2} = \sqrt{(750)^2 + (6700)^2} = 6742 \text{ N}$$

$$\theta = \tan^{-1} \frac{A_y}{A_x} = \tan^{-1} \frac{6700}{750} = \tan^{-1}(8.933) = 83.61^\circ \quad \Rightarrow \quad \mathbf{A} = 6740 \text{ N } \nearrow 83.6^\circ$$

$$+\curvearrowright \Sigma M_B = 0; \quad M_A + c A_x - a P = 0$$

$$\begin{aligned} \Rightarrow M_A &= -c A_x + a P = -(7.2 \text{ m}) (750 \text{ N}) + (2.1 \text{ m}) (900 \text{ N}) \\ &= -3510 \text{ N} \cdot \text{m} \quad \Rightarrow \quad \mathbf{M}_A = 3510 \text{ N} \cdot \text{m } \curvearrowleft \end{aligned}$$

R; (예: (a)와 (b)에서는 모멘트 식을 먼저 사용하지만, (c)에서는 힘 평형 식을 먼저 사용)

T; (예: 모멘트 반력 방향이 (b)에서는 반시계방향인데, (c)에서는 시계방향)