

[2.5절]

2.120 $W = 300 \text{ N}$, $\alpha = 30^\circ$, $\theta_A = 50^\circ$, $\theta_B = 40^\circ$, $\theta_C = 60^\circ$

S; known W , α , θ_A , θ_B , θ_C

M; FBD1

unknown T_{DA} , T_{DB} , T_{DC}

⇒ 공간에서 힘의 직각성분 (각도 이용)

A; FBD1에서 $\Sigma F_y = 0$, $P - W = 0$

$$\Rightarrow P = W = 300 \text{ N}$$

FBD2에서

$$(T_{DA})_y = -T_{DA} \cos\alpha, \quad (T_{DA})_h = T_{DA} \sin\alpha$$

$$(T_{DA})_x = -(T_{DA})_h \sin\theta_A = -T_{DA} \sin\alpha \sin\theta_A$$

$$(T_{DA})_z = (T_{DA})_h \cos\theta_A = T_{DA} \sin\alpha \cos\theta_A$$

$$(T_{DB})_y = -T_{DB} \cos\alpha, \quad (T_{DB})_h = T_{DB} \sin\alpha$$

$$(T_{DB})_x = (T_{DB})_h \cos\theta_B = T_{DB} \sin\alpha \cos\theta_B$$

$$(T_{DB})_z = (T_{DB})_h \sin\theta_B = T_{DB} \sin\alpha \sin\theta_B$$

$$(T_{DC})_y = -T_{DC} \cos\alpha, \quad (T_{DC})_h = T_{DC} \sin\alpha$$

$$(T_{DC})_x = (T_{DC})_h \cos\theta_C = T_{DC} \sin\alpha \cos\theta_C$$

$$(T_{DC})_z = -(T_{DC})_h \sin\theta_C = -T_{DC} \sin\alpha \sin\theta_C$$

$$\Sigma \mathbf{F} = 0 \Rightarrow \mathbf{P} + \mathbf{T}_{DA} + \mathbf{T}_{DB} + \mathbf{T}_{DC} = 0$$

$$\Sigma F_x = 0, \quad (T_{DA})_x + (T_{DB})_x + (T_{DC})_x = 0$$

$$-T_{DA} \sin\alpha \sin\theta_A + T_{DB} \sin\alpha \cos\theta_B + T_{DC} \sin\alpha \cos\theta_C = 0$$

$$-T_{DA} \sin\theta_A + T_{DB} \cos\theta_B + T_{DC} \cos\theta_C = 0$$

$$-T_{DA} \sin 50^\circ + T_{DB} \cos 40^\circ + T_{DC} \cos 60^\circ = 0$$

$$\Rightarrow -0.7660 T_{DA} + 0.7660 T_{DB} + 0.5 T_{DC} = 0 \quad \dots \textcircled{1}$$

$$\Sigma F_y = 0, \quad P + (T_{DA})_y + (T_{DB})_y + (T_{DC})_y = 0$$

$$T_{DA} \cos\alpha + T_{DB} \cos\alpha + T_{DC} \cos\alpha = P$$

$$T_{DA} + T_{DB} + T_{DC} = \frac{P}{\cos\alpha} = \frac{300 \text{ N}}{\cos 30^\circ}$$

$$\Rightarrow T_{DA} + T_{DB} + T_{DC} = 346.4 \text{ N} \quad \dots \textcircled{2}$$

$$\Sigma F_z = 0, \quad (T_{DA})_z + (T_{DB})_z + (T_{DC})_z = 0$$

$$T_{DA} \sin\alpha \cos\theta_A + T_{DB} \sin\alpha \sin\theta_B - T_{DC} \sin\alpha \sin\theta_C = 0$$

$$T_{DA} \cos\theta_A + T_{DB} \sin\theta_B - T_{DC} \sin\theta_C = 0$$

$$T_{DA} \cos 50^\circ + T_{DB} \sin 40^\circ - T_{DC} \sin 60^\circ = 0$$

$$\Rightarrow 0.6428 T_{DA} + 0.6428 T_{DB} - 0.8660 T_{DC} = 0 \quad \dots \textcircled{3}$$

$$\text{연립방정식 } \textcircled{1}, \textcircled{2}, \textcircled{3} \text{의 해} \Rightarrow T_{DA} = 147.6 \text{ N}, T_{DB} = 51.3 \text{ N}, T_{DC} = 147.6 \text{ N}$$

R; (과정의 타당성 서술) (가령, 방향여현 표현)

T; (결과의 의미 서술) (가령, $T_{DA} + T_{DB} + T_{DC} > W$ 인 이유)

