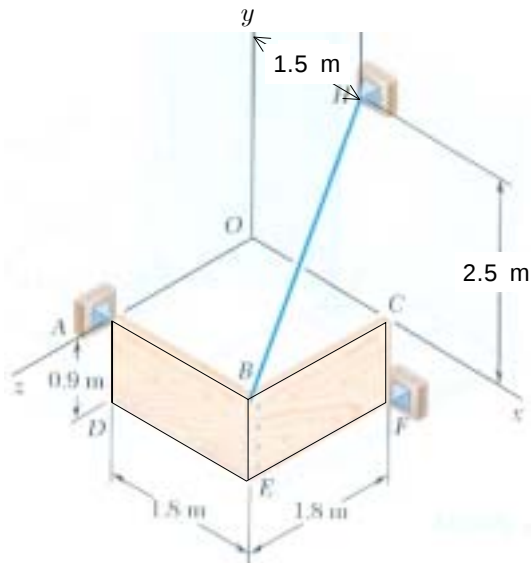


B $\mathcal{C}$



1.[8] 가 W 가
 A F -
 BH
 BH 55 N .



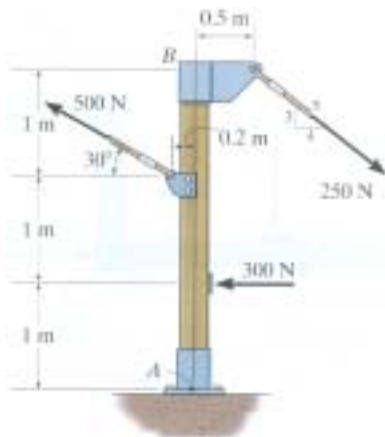
(a) $ABCFED$ (,)

(b) BH B 가

(c) T_{BH} A F

(d) 가
 A F
 M_{AF}

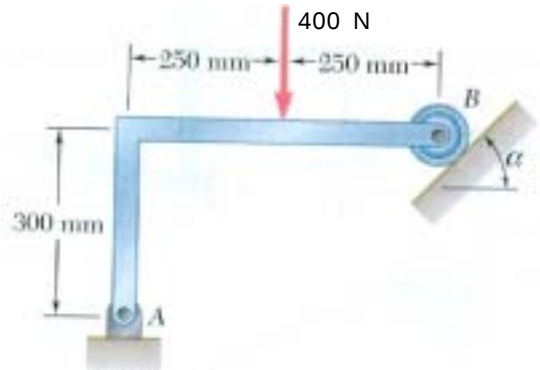
2.[4] 가
 A 가



(a) A 가 (,)

(b) A 가 (,)

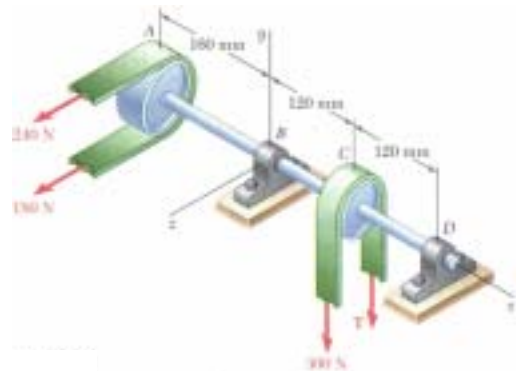
(3~4) The lever AB is hinged at A and is supported by a roller at B . The angle α is 35° . The weight of the lever is negligible.



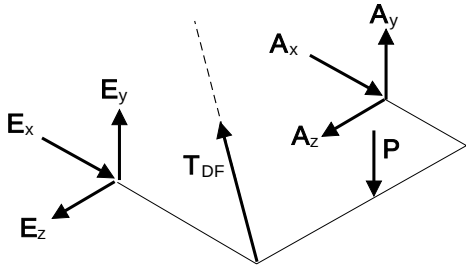
3.[6]
 B () , A

4.[5] (force triangle)
 A

5.[2] Two transmission belts pass over a double-sheaved pulley that is attached to an axle supported by bearings at B and D . Assume that the bearings are thin and that they do not exert any axial force. Express reactions at B and D .



1. (a)



(b) $T_{DF} = 840 \text{ N}$

$DF ; \quad d_x = -160 \text{ mm}, \quad d_y = 110 \text{ mm}, \quad d_z = -80 \text{ mm}$

$$\lambda_{DF} = \frac{(-160 \text{ mm})\mathbf{i} + (110 \text{ mm})\mathbf{j} + (-80 \text{ mm})\mathbf{k}}{\sqrt{(-160 \text{ mm})^2 + (110 \text{ mm})^2 + (-80 \text{ mm})^2}} = \frac{1}{210} [(-160)\mathbf{i} + (110)\mathbf{j} + (-80)\mathbf{k}]$$

$$\begin{aligned} \mathbf{T}_{DF} &= T_{DF} \lambda_{DF} = (840 \text{ N}) \frac{1}{21} [(-16)\mathbf{i} + (11)\mathbf{j} + (-8)\mathbf{k}] \\ &= (-640 \text{ N}) \mathbf{i} + (440 \text{ N}) \mathbf{j} + (-320 \text{ N}) \mathbf{k} \end{aligned}$$

(c) $\mathbf{r}_{D/E} = (160 \text{ mm}) \mathbf{i}, \quad \mathbf{r}_{D/A} = (90 \text{ mm}) \mathbf{i} + (240 \text{ mm}) \mathbf{k}, \quad \mathbf{r}_{F/E} = (110 \text{ mm}) \mathbf{j} + (-80 \text{ mm}) \mathbf{k},$
 $\mathbf{r}_{F/A} = (-70 \text{ mm}) \mathbf{i} + (110 \text{ mm}) \mathbf{j} + (160 \text{ mm}) \mathbf{k}$

(d) $\lambda_{AE} = \frac{(-70 \text{ mm})\mathbf{i} + (240 \text{ mm})\mathbf{k}}{\sqrt{(-70 \text{ mm})^2 + (240 \text{ mm})^2}} = \frac{1}{250} [(-70)\mathbf{i} + (240)\mathbf{k}] = -0.28 \mathbf{i} + 0.96 \mathbf{k}$

$\mathbf{r}_{D/E} = (160 \text{ mm}) \mathbf{i} = (0.160 \text{ m}) \mathbf{i}$

$$\begin{aligned} \mathbf{r}_{D/E} \times \mathbf{T}_{DF} &= [(0.160 \text{ m}) \mathbf{i}] \times [(-640 \text{ N}) \mathbf{i} + (440 \text{ N}) \mathbf{j} + (-320 \text{ N}) \mathbf{k}] \\ &= (0.160 \text{ m})(440 \text{ N}) \mathbf{k} - (0.160 \text{ m})(-320 \text{ N}) \mathbf{j} = 51.2 \mathbf{j} + 70.4 \mathbf{k} \quad (\text{N}\cdot\text{m}) \end{aligned}$$

$$\begin{aligned} M_{AE} &= \lambda_{AE} \cdot (\mathbf{r}_{D/E} \times \mathbf{T}_{DF}) \\ &= (-0.28 \mathbf{i} + 0.96 \mathbf{k}) \cdot (51.2 \mathbf{j} + 70.4 \mathbf{k}) \quad (\text{N}\cdot\text{m}) = (0.96)(70.4) \quad (\text{N}\cdot\text{m}) = 67.584 \quad (\text{N}\cdot\text{m}) \\ M_{AE} &= 67.6 \text{ N}\cdot\text{m} \end{aligned}$$

2. (a) $R_x = \Sigma F_x = (500 \text{ N}) \frac{3}{5} = 300 \text{ N}, \quad R_y = \Sigma F_y = (-750 \text{ N}) + (500 \text{ N}) \frac{4}{5} = -350 \text{ N}$

$$R = \sqrt{R_x^2 + R_y^2} = \sqrt{(300 \text{ N})^2 + (-350 \text{ N})^2} = 461.0 \text{ N}$$

$$\tan \theta = \frac{R_y}{R_x} = \frac{-350}{300} = -1.1667 \quad \theta = \tan^{-1}(-1.1667) = -49.40^\circ$$

$$\mathbf{R} = 461 \text{ N} \quad \nwarrow 49.4^\circ$$

(b) $M_O = \Sigma M = -(1.25 \text{ m})(750 \text{ N}) + (2.50 \text{ m})(400 \text{ N}) - (1 \text{ m})(300 \text{ N}) + (1 \text{ m})(200 \text{ N})$
 $= -37.5 \text{ N}\cdot\text{m}$

$$\mathbf{M}_O = 37.5 \text{ N}\cdot\text{m} \quad \uparrow$$

3. $P = 300 \text{ N}$

$$\tan \theta = \frac{3}{4}$$

$$\theta = \tan^{-1}(0.75) = 36.87^\circ$$

$$d_1 = (105 \text{ mm}) \tan \theta$$

$$= (105 \text{ mm})(0.75) = 78.75 \text{ mm}$$

$$d_2 = (40 \text{ mm}) + d_1$$

$$= (40 \text{ mm}) + (78.75 \text{ mm}) = 118.75 \text{ mm}$$

$$\alpha = \tan^{-1} \frac{75 \text{ mm}}{d_2} = \tan^{-1} \frac{75 \text{ mm}}{118.75 \text{ mm}}$$

$$= \tan^{-1}(0.6316) = 32.28^\circ$$

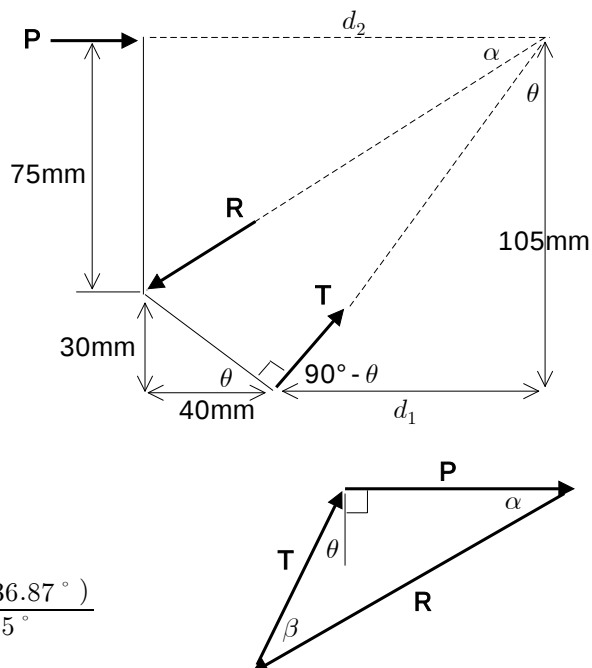
$$\beta = 180^\circ - 32.28^\circ - (90^\circ + 36.87^\circ) = 20.85^\circ$$

$$\frac{R}{\sin(90^\circ + \theta)} = \frac{P}{\sin \beta}$$

$$R = P \frac{\sin(90^\circ + \theta)}{\sin \beta} = (300 \text{ N}) \frac{\sin(90^\circ + 36.87^\circ)}{\sin 20.85^\circ}$$

$$= 674.3 \text{ N}$$

$$R = 674 \text{ N} \angle 32.3^\circ$$



4. $W = 150 \text{ N}$

$$\Sigma M_x = 0;$$

$$-A_y (1.2 \text{ m}) - B_y (0.9 \text{ m}) + W (0.6 \text{ m}) = 0 \quad \dots$$

$$\Sigma M_{Cz} = 0;$$

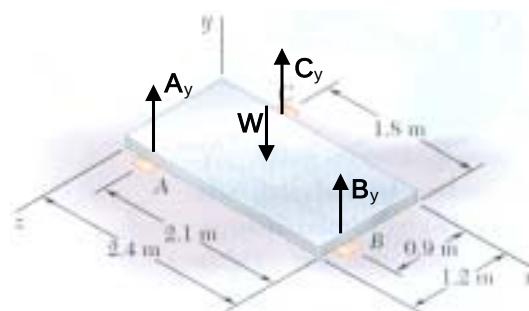
$$-A_y (0.3 \text{ m}) + B_y (1.8 \text{ m}) - W (0.6 \text{ m}) = 0 \quad \dots$$

$$\times 2 +$$

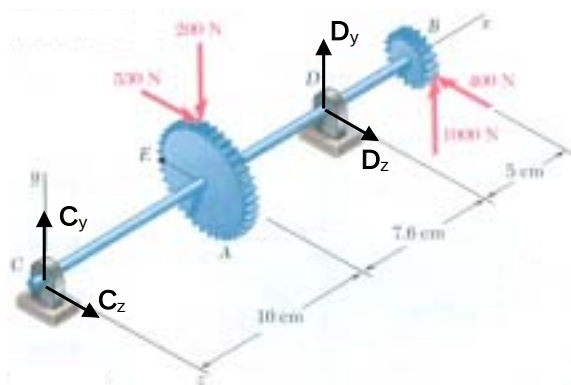
$$-A_y (1.2 \times 2 + 0.3) + W (0.6 \times 2 - 0.6) = 0$$

$$A_y = W \frac{0.6 \times 2 - 0.6}{1.2 \times 2 + 0.3} = (150 \text{ N}) \frac{0.6}{2.7} = 33.3 \text{ N}$$

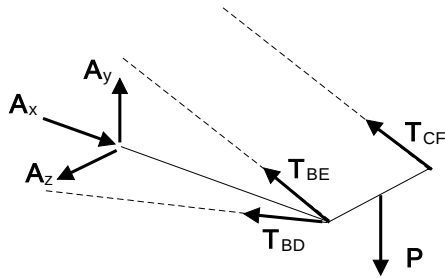
$$A = 33.3 \text{ N} \uparrow$$



5.



1. (a)



(b) $T_{BE} = 1.25 \text{ kN}$

$$BE; \quad d_x = -152 \text{ cm}, \quad d_y = 63.5 \text{ cm}, \quad d_z = 0$$

$$\lambda_{BE} = \frac{(-152 \text{ cm})\mathbf{i} + (63.5 \text{ cm})\mathbf{j} + (0)\mathbf{k}}{\sqrt{(-152 \text{ cm})^2 + (63.5 \text{ cm})^2 + 0}} = \frac{1}{164.73} [(-152)\mathbf{i} + (63.5)\mathbf{j}]$$

$$\begin{aligned} \mathbf{T}_{BE} &= T_{BE} \lambda_{BE} = (1.25 \text{ kN}) \frac{1}{164.73} [(-152)\mathbf{i} + (63.5)\mathbf{j}] \\ &= (-1.153 \text{ kN}) \mathbf{i} + (0.482 \text{ kN}) \mathbf{j} \end{aligned}$$

(c) $\mathbf{r}_{B/A} = (152 \text{ cm}) \mathbf{i}$, $\mathbf{r}_{E/A} = (63.5 \text{ cm}) \mathbf{j}$, $\mathbf{r}_{E/F} = (-76 \text{ cm}) \mathbf{k}$,
 $\mathbf{r}_{B/F} = (152 \text{ cm}) \mathbf{i} + (-63.5 \text{ cm}) \mathbf{j} + (76 \text{ cm}) \mathbf{k}$

$$(d) \lambda_{AF} = \frac{(63.5 \text{ cm})\mathbf{j} + (-76 \text{ cm})\mathbf{k}}{\sqrt{(63.5 \text{ cm})^2 + (-76 \text{ cm})^2}} = \frac{1}{99.0} [(63.5)\mathbf{j} + (-76)\mathbf{k}] = 0.641 \mathbf{j} - 0.767 \mathbf{k}$$

$$\mathbf{r}_{B/A} = (152 \text{ cm}) \mathbf{i} = (1.52 \text{ m}) \mathbf{i}$$

$$\begin{aligned} \mathbf{r}_{B/A} \times \mathbf{T}_{BE} &= [(1.52 \text{ m}) \mathbf{i}] \times [(-1.153 \text{ kN}) \mathbf{i} + (0.482 \text{ kN}) \mathbf{j}] \\ &= (1.52 \text{ m})(0.482 \text{ kN}) \mathbf{k} = 0.7326 \text{ k N}\cdot\text{m} = 732.6 \text{ k N}\cdot\text{m} \end{aligned}$$

$$\begin{aligned} M_{AF} &= \lambda_{AF} \cdot (\mathbf{r}_{B/A} \times \mathbf{T}_{BE}) \\ &= (0.641 \mathbf{j} - 0.767 \mathbf{k}) \cdot (732.6 \text{ k N}\cdot\text{m}) = (-0.767)(732.6) (\text{N}\cdot\text{m}) = -561.9 (\text{N}\cdot\text{m}) \\ M_{AF} &= -562 \text{ N}\cdot\text{m} \end{aligned}$$

$$2. (a) R_x = \Sigma F_x = (750 \text{ N}) \frac{3}{5} + (250 \text{ N}) - (500 \text{ N}) \frac{4}{5} = 300 \text{ N}$$

$$R_y = \Sigma F_y = -(750 \text{ N}) \frac{4}{5} - (500 \text{ N}) \frac{3}{5} = -900 \text{ N}$$

$$R = \sqrt{R_x^2 + R_y^2} = \sqrt{(300 \text{ N})^2 + (-900 \text{ N})^2} = 948.7 \text{ N}$$

$$\tan \theta = \frac{R_y}{R_x} = \frac{-900}{300} = -3.00 \quad \theta = \tan^{-1}(-3.00) = -71.57^\circ$$

$$\mathbf{R} = 949 \text{ N} \angle -71.6^\circ$$

$$(b) M_A = \Sigma M = -(0.9 \text{ m})(750 \text{ N}) \frac{4}{5} - (1.8 \text{ m})(500 \text{ N}) \frac{3}{5} + (0.3 \text{ m})(500 \text{ N}) \frac{4}{5}$$

$$= -960.0 \text{ N}\cdot\text{m}$$

$$\mathbf{M}_A = 960 \text{ N}\cdot\text{m} \uparrow$$

3. $F_A = 18 \text{ N}$, $\alpha = 30^\circ$, $\delta = 0.09 \text{ m}$
 $d_1 = 0.06 \text{ m}$, $d_2 = 0.036 \text{ m}$, $d_3 = 0.022 \text{ m}$

$$+\uparrow \Sigma M_B = 0 ;$$

$$F_A \frac{d_1}{\cos \alpha} - F_C d_3 = 0$$

$$F_C = F_A \frac{d_1}{d_3 \cos \alpha} = (18 \text{ N}) \frac{0.06 \text{ m}}{(0.022 \text{ m}) \cos 30^\circ} = 56.69 \text{ N}$$

$$F_C = 56.7 \text{ N} \rightarrow$$

$$\rightarrow \Sigma F_x = 0 ; \quad F_A \sin \alpha + B_x + F_C = 0$$

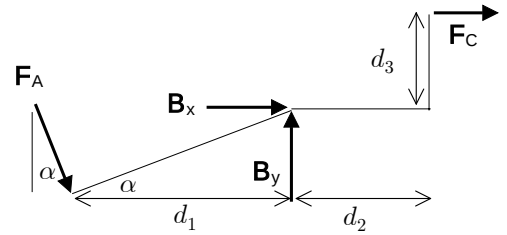
$$B_x = -F_A \sin \alpha - F_C = -(18 \text{ N}) \sin 30^\circ - (56.69 \text{ N}) = -65.69 \text{ N}$$

$$B_x = 65.7 \text{ N} \leftarrow$$

$$\uparrow \Sigma F_y = 0 ; \quad -F_A \cos \alpha + B_y = 0$$

$$B_y = F_A \cos \alpha = (18 \text{ N}) \cos 30^\circ = 15.59 \text{ N}$$

$$B_y = 15.59 \text{ N} \uparrow$$



4. $F_A = 18 \text{ N}$, $\alpha = 30^\circ$, $\delta = 0.03 \text{ m}$

$$d_{EF} = (2.2 \text{ cm}) + (6 \text{ cm}) \tan \alpha$$

$$= (2.2 \text{ cm}) + (6 \text{ cm}) \tan 30^\circ$$

$$= 5.664 \text{ cm}$$

$$d_{AF} = d_{EF} \tan \alpha$$

$$= (5.664 \text{ cm}) \tan 30^\circ = 3.270 \text{ cm}$$

$$\tan \theta = \frac{(2.2 \text{ cm})}{d_{AF} + (6 \text{ cm})} = \frac{(2.2 \text{ cm})}{(3.270 \text{ cm}) + (6 \text{ cm})}$$

$$= 0.2373$$

$$\theta = \tan^{-1}(0.2373) = 13.35^\circ$$

$$\gamma = 90^\circ + \alpha = 90^\circ + 30^\circ = 120^\circ$$

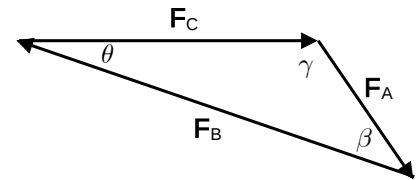
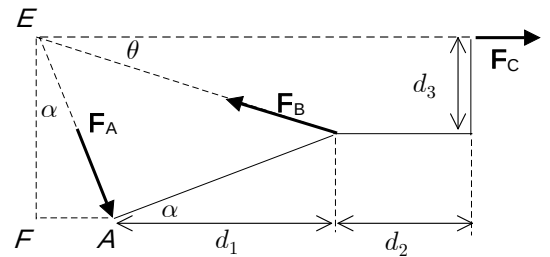
$$\beta = 180^\circ - \gamma - \theta$$

$$= 180^\circ - 120^\circ - 13.35^\circ = 46.65^\circ$$

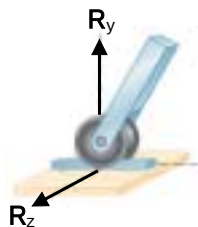
$$\frac{F_A}{\sin \theta} = \frac{F_B}{\sin \gamma}$$

$$F_B = P_A \frac{\sin \gamma}{\sin \theta} = (18 \text{ N}) \frac{\sin 120^\circ}{\sin 13.35^\circ} = 67.51 \text{ N}$$

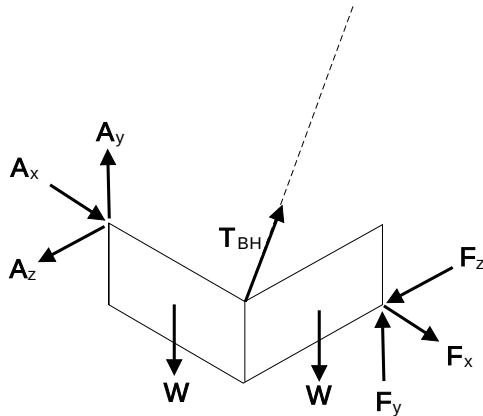
$$F_B = 67.5 \text{ N} \angle 13.35^\circ$$



- 5.



1. (a)



(b) $T_{BH} = 55 \text{ N}$

BH ; $d_x = -0.3 \text{ m}$, $d_y = 2.5 \text{ m}$, $d_z = -1.8 \text{ m}$

$$\lambda_{BH} = \frac{(-0.3 \text{ m})\mathbf{i} + (2.5 \text{ m})\mathbf{j} + (-1.8 \text{ m})\mathbf{k}}{\sqrt{(-0.3 \text{ m})^2 + (2.5 \text{ m})^2 + (-1.8 \text{ m})^2}} = \frac{1}{3.095} [(-0.3)\mathbf{i} + (2.5)\mathbf{j} + (-1.8)\mathbf{k}]$$

$$\begin{aligned} \mathbf{T}_{BH} &= T_{BH} \lambda_{BH} = (55 \text{ N}) \frac{1}{3.095} [(-0.3)\mathbf{i} + (2.5)\mathbf{j} + (-1.8)\mathbf{k}] \\ &= (-5.33 \text{ N}) \mathbf{i} + (44.4 \text{ N}) \mathbf{j} + (-32.0 \text{ N}) \mathbf{k} \end{aligned}$$

(c) $\mathbf{r}_{B/A} = (1.8 \text{ m}) \mathbf{i}$, $\mathbf{r}_{B/F} = (0.9 \text{ m}) \mathbf{j} + (1.8 \text{ m}) \mathbf{k}$, $\mathbf{r}_{H/F} = (-0.3 \text{ m}) \mathbf{i} + (3.4 \text{ m}) \mathbf{j}$,
 $\mathbf{r}_{H/A} = (1.5 \text{ m}) \mathbf{i} + (2.5 \text{ m}) \mathbf{j} + (-1.8 \text{ m}) \mathbf{k}$

$$\begin{aligned} \text{(d)} \lambda_{AF} &= \frac{(1.8 \text{ m})\mathbf{i} + (-0.9 \text{ m})\mathbf{j} + (-1.8 \text{ m})\mathbf{k}}{\sqrt{(1.8 \text{ m})^2 + (-0.9 \text{ m})^2 + (-1.8 \text{ m})^2}} = \frac{1}{2.7} [(1.8)\mathbf{i} + (-0.9)\mathbf{j} + (-1.8)\mathbf{k}] \\ &= 0.6667 \mathbf{i} - 0.3333 \mathbf{j} - 0.6667 \mathbf{k} \end{aligned}$$

$$\mathbf{r}_{B/A} = (1.8 \text{ m}) \mathbf{i}$$

$$\begin{aligned} \mathbf{r}_{B/A} \times \mathbf{T}_{BH} &= [(1.8 \text{ m}) \mathbf{i}] \times [(-5.33 \text{ N}) \mathbf{i} + (44.4 \text{ N}) \mathbf{j} + (-32.0 \text{ N}) \mathbf{k}] \\ &= (1.8 \text{ m})(44.4 \text{ N}) \mathbf{k} - (1.8 \text{ m})(-32.0 \text{ N}) \mathbf{j} = 57.60 \mathbf{j} + 79.92 \mathbf{k} \text{ N}\cdot\text{m} \end{aligned}$$

$$\begin{aligned} M_{AF} &= \lambda_{AF} \cdot (\mathbf{r}_{B/A} \times \mathbf{T}_{BH}) \\ &= (0.6667 \mathbf{i} - 0.3333 \mathbf{j} - 0.6667 \mathbf{k}) \cdot (57.60 \mathbf{j} + 79.92 \mathbf{k}) \text{ (N}\cdot\text{m)} \\ &= (-0.3333)(57.60) + (-0.6667)(79.92) \text{ (N}\cdot\text{m)} = -72.48 \text{ (N}\cdot\text{m)} \\ M_{AF} &= -72.5 \text{ N}\cdot\text{m} \end{aligned}$$

$$2. \text{ (a)} R_x = \Sigma F_x = (250 \text{ N}) \frac{4}{5} - (300 \text{ N}) - (500 \text{ N}) \cos 30^\circ = -533 \text{ N}$$

$$R_y = \Sigma F_y = -(250 \text{ N}) \frac{3}{5} + (500 \text{ N}) \sin 30^\circ = 100 \text{ N}$$

$$R = \sqrt{R_x^2 + R_y^2} = \sqrt{(-533 \text{ N})^2 + (100 \text{ N})^2} = 542.3 \text{ N}$$

$$\tan \theta = \frac{R_y}{R_x} = \frac{100}{-533} = -0.1876 \quad \theta = \tan^{-1}(-0.1876) = -10.63^\circ$$

$$\mathbf{R} = 543 \text{ N} \angle -10.6^\circ$$

$$\text{(b)} M_A = \Sigma M = -(3 \text{ m})(250 \text{ N}) \frac{4}{5} - (0.5 \text{ m})(250 \text{ N}) \frac{3}{5} + (1 \text{ m})(300 \text{ N})$$

$$+ (2 \text{ m})(500 \text{ N}) \cos 30^\circ - (0.2 \text{ m})(500 \text{ N}) \sin 30^\circ = 441.0 \text{ N}\cdot\text{m}$$

$$\mathbf{M}_A = 441 \text{ N}\cdot\text{m} \uparrow$$

3. $P = 400 \text{ N}$, $a = 0.3 \text{ m}$, $b = 0.25 \text{ m}$, $\alpha = 35^\circ$

$$+\uparrow \Sigma M_A = 0 ;$$

$$-b P + a (B \sin \alpha) + 2b (B \cos \alpha) = 0$$

$$B = P \frac{b}{a \sin \alpha + 2b \cos \alpha}$$

$$= (400 \text{ N}) \frac{0.25 \text{ m}}{(0.3 \text{ m}) \sin 35^\circ + 2(0.25 \text{ m}) \cos 35^\circ}$$

$$= 171.93 \text{ N} \quad \mathbf{B} = 171.9 \text{ N } \underline{55^\circ}$$

$$\rightarrow \Sigma F_x = 0 ;$$

$$A_x - B \sin \alpha = 0$$

$$A_x = B \sin \alpha = (171.93 \text{ N}) \sin 35^\circ = 98.61 \text{ N}$$

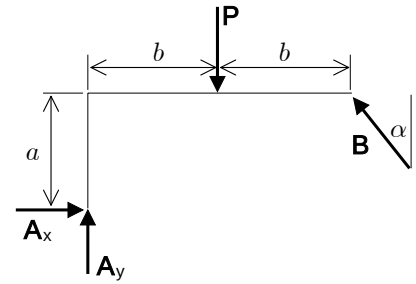
$$\mathbf{A}_x = 98.6 \text{ N } \rightarrow$$

$$\uparrow \Sigma F_y = 0 ;$$

$$A_y - P + B \cos \alpha = 0$$

$$A_y = P - B \cos \alpha = (400 \text{ N}) - (171.93 \text{ N}) \cos 35^\circ = 259.2 \text{ N}$$

$$\mathbf{A}_y = 259 \text{ N } \uparrow$$



4. $\alpha = 35^\circ$, $P = 400 \text{ N}$

$$d_{BC} = 0.25 \text{ m}, \quad d_{CE} = 0.25 \text{ m}, \quad d_{AE} = 0.3 \text{ m}$$

$$d_{EF} = d_{CD} = \frac{d_{BC}}{\tan \alpha} = \frac{0.25 \text{ m}}{\tan 35^\circ} = 0.357 \text{ m}$$

$$d_{AF} = d_{AE} + d_{EF} = (0.3 \text{ m}) + (0.357 \text{ m}) = 0.657 \text{ m}$$

$$\tan \theta = \frac{d_{DF}}{d_{AF}} = \frac{0.25 \text{ m}}{0.657 \text{ m}} = 0.3805$$

$$\theta = \tan^{-1}(0.3805) = 20.83^\circ$$

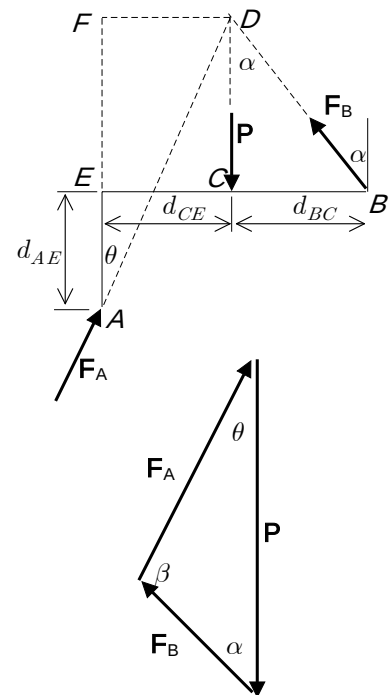
$$\beta = 180^\circ - \alpha - \theta = 180^\circ - 35^\circ - 20.83^\circ = 124.17^\circ$$

$$\frac{F_A}{\sin \alpha} = \frac{P}{\sin \beta}$$

$$F_A = P \frac{\sin \alpha}{\sin \beta} = (400 \text{ N}) \frac{\sin 35^\circ}{\sin 124.17^\circ} = 277.3 \text{ N}$$

$$180^\circ - \theta = 90^\circ - 20.83^\circ = 69.17^\circ$$

$$\mathbf{F}_A = 277 \text{ N } \underline{69.2^\circ}$$



5.

