

<2.12~2.14 >

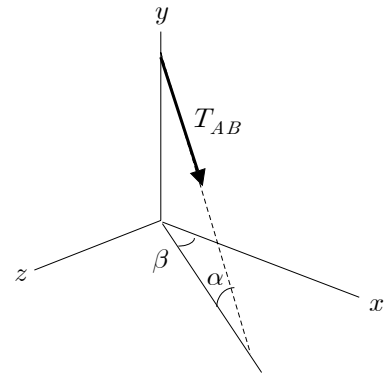
2.75 $T_{AB} = 4.2 \text{ kN}, \quad \alpha = 40^\circ, \quad \beta = 40^\circ$

(a) $F_y = -T_{AB} \sin\alpha$
 $= -(4.2 \text{ kN}) \sin 40^\circ = -2.6997 \text{ kN}$

$F_x = (T_{AB} \cos\alpha) \cos\beta$
 $= (4.2 \text{ kN}) \cos 40^\circ \cos 40^\circ$
 $= 2.4647 \text{ kN}$

$F_z = (T_{AB} \cos\alpha) \sin\beta$
 $= (4.2 \text{ kN}) \cos 40^\circ \sin 40^\circ$
 $= 2.0681 \text{ kN}$

$F_x = 2.46 \text{ kN}, \quad F_y = -2.70 \text{ kN}, \quad F_z = 2.07 \text{ kN}$

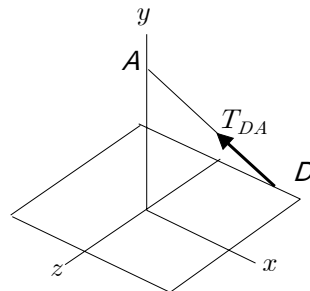


(b) $\cos\theta_x = \frac{F_x}{T_{AB}} = \frac{2.4647}{4.2} = 0.58683$ $\theta_x = \cos^{-1}0.58683 = 54.1^\circ$

$\cos\theta_y = \frac{F_y}{T_{AB}} = \frac{-2.6997}{4.2} = -0.64279$ $\theta_y = \cos^{-1}(-0.67279) = 130.0^\circ$

$\cos\theta_z = \frac{F_z}{T_{AB}} = \frac{2.0681}{4.2} = 0.49240$ $\theta_z = \cos^{-1}0.49240 = 60.5^\circ$

2.90



$T_{DA} = 870 \text{ N}$

$\mathbf{d} = (-0.6 \text{ m})\mathbf{i} + (1.2 \text{ m})\mathbf{j} + (0.9 \text{ m})\mathbf{k}$

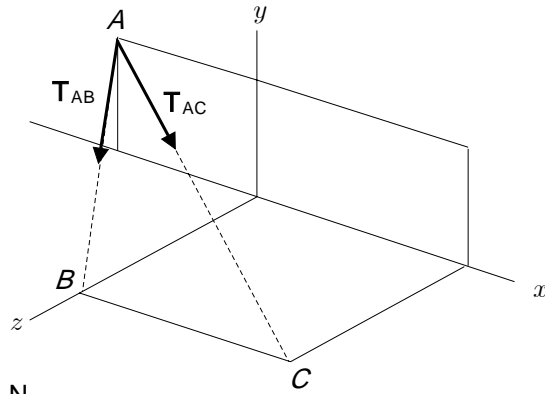
$d = \sqrt{(-0.6 \text{ m})^2 + (1.2 \text{ m})^2 + (0.9 \text{ m})^2} = 1.6155 \text{ m}$

$\lambda = \frac{\mathbf{d}}{d} = \frac{1}{1.6155 \text{ m}} [(-0.6 \text{ m})\mathbf{i} + (1.2 \text{ m})\mathbf{j} + (0.9 \text{ m})\mathbf{k}]$
 $= -0.3714 \mathbf{i} + 0.74278 \mathbf{j} + 0.5571 \mathbf{k}$

$\mathbf{F}_{DA} = T_{DA} \lambda$
 $= (870 \text{ N}) (-0.3714 \mathbf{i} + 0.74278 \mathbf{j} + 0.5571 \mathbf{k})$
 $= (-323.1 \text{ N}) \mathbf{i} + (646.2 \text{ N}) \mathbf{j} + (484.7 \text{ N}) \mathbf{k}$

$F_x = (-323 \text{ N}) \mathbf{i}, \quad F_y = (646 \text{ N}) \mathbf{j}, \quad F_z = (485 \text{ N}) \mathbf{k}$

2.95



$$T_{AB} = 850 \text{ N}$$

$$\mathbf{d}_{AB} = (0.40 \text{ m})\mathbf{i} + (-0.45 \text{ m})\mathbf{j} + (0.60 \text{ m})\mathbf{k}$$

$$d_{AB} = \sqrt{(0.40 \text{ m})^2 + (-0.45 \text{ m})^2 + (0.60 \text{ m})^2} = 0.850 \text{ m}$$

$$\begin{aligned} \lambda_{AB} &= \frac{\mathbf{d}_{AB}}{d_{AB}} = \frac{1}{0.850 \text{ m}} [(0.40 \text{ m})\mathbf{i} + (-0.45 \text{ m})\mathbf{j} + (0.60 \text{ m})\mathbf{k}] \\ &= 0.4706 \mathbf{i} - 0.5294 \mathbf{j} + 0.7059 \mathbf{k} \end{aligned}$$

$$\begin{aligned} \mathbf{T}_{AB} &= T_{AB} \lambda_{AB} \\ &= (850 \text{ N}) (0.4706 \mathbf{i} - 0.5294 \mathbf{j} + 0.7059 \mathbf{k}) \\ &= (400 \text{ N}) \mathbf{i} + (-450 \text{ N}) \mathbf{j} + (600 \text{ N}) \mathbf{k} \end{aligned}$$

$$T_{AC} = 1020 \text{ N}$$

$$\mathbf{d}_{AC} = (1.00 \text{ m})\mathbf{i} + (-0.45 \text{ m})\mathbf{j} + (0.60 \text{ m})\mathbf{k}$$

$$d_{AC} = \sqrt{(1.00 \text{ m})^2 + (-0.45 \text{ m})^2 + (0.60 \text{ m})^2} = 1.250 \text{ m}$$

$$\begin{aligned} \lambda_{AC} &= \frac{\mathbf{d}_{AC}}{d_{AC}} = \frac{1}{1.250 \text{ m}} [(1.00 \text{ m})\mathbf{i} + (-0.45 \text{ m})\mathbf{j} + (0.60 \text{ m})\mathbf{k}] \\ &= 0.800 \mathbf{i} - 0.360 \mathbf{j} + 0.480 \mathbf{k} \end{aligned}$$

$$\begin{aligned} \mathbf{T}_{AC} &= T_{AC} \lambda_{AC} \\ &= (1020 \text{ N}) (0.800 \mathbf{i} - 0.360 \mathbf{j} + 0.480 \mathbf{k}) \\ &= (816.0 \text{ N}) \mathbf{i} + (-367.2 \text{ N}) \mathbf{j} + (489.6 \text{ N}) \mathbf{k} \end{aligned}$$

$$\begin{aligned} \mathbf{R} &= \mathbf{T}_{AB} + \mathbf{T}_{AC} \\ &= [(400 \text{ N}) \mathbf{i} + (-450 \text{ N}) \mathbf{j} + (600 \text{ N}) \mathbf{k}] \\ &\quad + [(816.0 \text{ N}) \mathbf{i} + (-367.2 \text{ N}) \mathbf{j} + (489.6 \text{ N}) \mathbf{k}] \\ &= (1216.0 \text{ N}) \mathbf{i} + (-817.2 \text{ N}) \mathbf{j} + (1089.6 \text{ N}) \mathbf{k} \end{aligned}$$

$$\begin{aligned} R &= \sqrt{R_x^2 + R_y^2 + R_z^2} = \sqrt{(1216.0 \text{ N})^2 + (-817.2 \text{ N})^2 + (1089.6 \text{ N})^2} = 1825.8 \text{ N} \\ R &= 1826 \text{ N} \end{aligned}$$

$$\cos \theta_x = \frac{R_x}{R} = \frac{1216.0}{1825.8} = 0.66601 \quad \theta_x = \cos^{-1} 0.66601 = 48.2^\circ$$

$$\cos \theta_y = \frac{R_y}{R} = \frac{-817.2}{1825.8} = -0.44758 \quad \theta_y = \cos^{-1} (-0.44758) = 116.6^\circ$$

$$\cos \theta_z = \frac{R_z}{R} = \frac{1089.6}{1825.8} = 0.59678 \quad \theta_z = \cos^{-1} 0.59678 = 53.4^\circ$$